

Mixture and Alligation



~ Quantitative Aptitude · SSC Exams ~

← the "cross" rule solves half of these in seconds!



This chapter blends two or more ingredients and asks for the **ratio, mean value or strength** of the result. One tool — the **alligation cross** — runs through it all.

① Mean Price / Mean Value

When quantities are mixed, the **mean price** is the cost price of **one unit** (1 kg, 1 L...) of the final mixture.

Mean price = (Total cost of all ingredients) / (Total quantity)

Each ingredient's cost = its rate × its quantity. Add them, then divide by the total quantity.

Worked example — mixing two sugars

Given — 3 kg sugar at ₹40/kg mixed with 2 kg at ₹50/kg.

Total cost → $3 \times 40 + 2 \times 50 = 120 + 100 = ₹220$.

Total quantity → $3 + 2 = 5$ kg.

Mean price → $220 \div 5 = ₹44/\text{kg}$. 

Worked example — three-item mixture

5 L oil at ₹90 + 3 L at ₹100 + 2 L at ₹120.

Cost = $450 + 300 + 240 = ₹990$; quantity = 10 L ∴ mean = $990 \div 10 = ₹99/\text{L}$.

Try these

2 kg @ ₹30 + 3 kg @ ₹40 → **₹36**

4 L @ ₹25 + 1 L @ ₹50 → **₹30**

1 kg @ ₹60 + 1 kg @ ₹80 → **₹70**

6 kg @ ₹15 + 4 kg @ ₹20 → **₹17**



The mean price always lies **between** the cheapest and dearest rate — if your answer falls outside that band, something is wrong.

② The Rule of Alligation

Alligation reverses the mean-price idea: given the two rates and the mean, it finds the **ratio** in which they must be mixed.

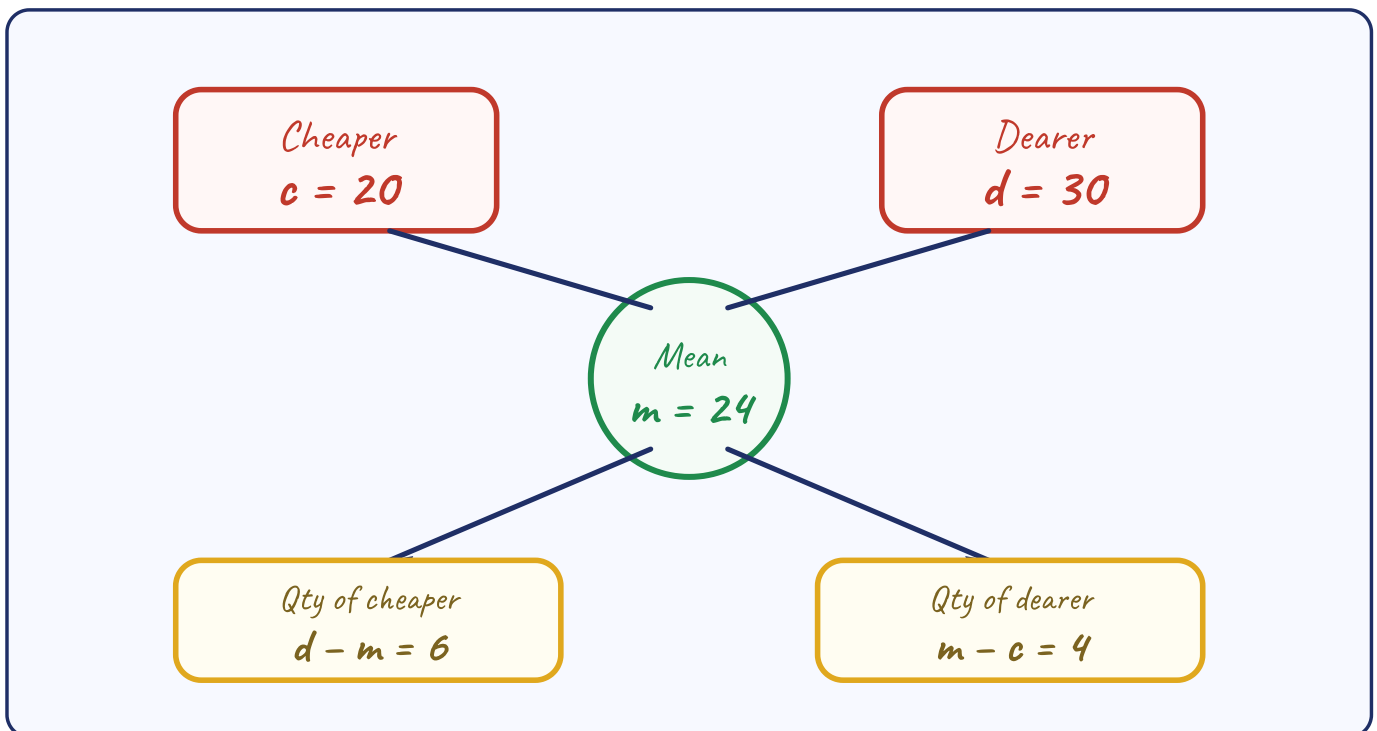
Rule of Alligation

If ingredients of value c (cheaper) and d (dearer) are mixed to a mean value m , then

$$(\text{Qty of cheaper}) : (\text{Qty of dearer}) = (d - m) : (m - c)$$

Each ratio-part is the **difference across the diagonal** — hence the "cross".

The cross — how to draw it



- Put c and d at the two **top** corners, the mean m in the **middle**.
- Subtract **diagonally**: $d - m$ sits under c , and $m - c$ sits under d .
- Read the bottom row: cheaper : dearer = $(d - m) : (m - c)$. Always keep the answer positive.



The part written under an ingredient is **its own share**. Under the cheaper you get $(d - m)$ — the quantity of the cheaper.

Alligation – Worked Examples

Worked example 1 – the rice mix

Given – rice at ₹20/kg and ₹30/kg mixed to cost ₹24/kg.

Cross → $c = 20, d = 30, m = 24$.

Cheaper = $d - m = 30 - 24 = 6$; **Dearer** = $m - c = 24 - 20 = 4$.

Ratio → $6 : 4 = 3 : 2$ (cheaper : dearer). ✓

Worked example 2 – two teas

Tea at ₹18 and ₹24 mixed to sell (mean) at ₹20/kg. $c = 18, d = 24, m = 20$.

Cheaper : Dearer = $(24-20) : (20-18) = 4 : 2 = 2 : 1$.

So for every 2 kg of the ₹18 tea, take 1 kg of the ₹24 tea.

Worked example 3 – find the quantity

In what quantity must ₹16 wheat be mixed with 12 kg of ₹24 wheat to make the mean ₹18/kg?

Ratio = $(24-18):(18-16) = 6:2 = 3:1$ (cheaper:dearer).

Dearer = 12 kg is the "1" part → cheaper = 3 parts = 36 kg. ✓

Worked example 4 – ratio to percentage

Two salts at ₹12 and ₹18 give a mean of ₹14. Ratio = $(18-14):(14-12) = 4:2 = 2:1$.

Cheaper is 2 of 3 parts → it forms $66\frac{2}{3}\%$ of the mixture, dearer $33\frac{1}{3}\%$.

Try these (cheaper : dearer)

₹10, ₹15, mean ₹12 → $3 : 2$

₹25, ₹40, mean ₹30 → $2 : 1$

₹8, ₹12, mean ₹9 → $3 : 1$

₹50, ₹70, mean ₹65 → $1 : 3$



The bigger the gap between the mean and a rate, the less of that ingredient you need – the diagonal difference is small on the near side.

③ Reverse Alligation

The same cross runs **backwards**: if the **ratio** is known you can find the **mean**, or if the mean and one rate are known you can find the **missing rate**.

Mean from a known ratio

Mean value $m = (c \cdot q_c + d \cdot q_d) / (q_c + q_d)$ — the weighted average of the two rates.

Worked example 1 — find the mean

Given — mix ₹25 and ₹30 sugar in the ratio 2 : 3.

Mean → $(25 \times 2 + 30 \times 3) / (2 + 3) = (50 + 90) / 5 = 140 / 5 = \text{₹}28/\text{kg}$. ✓

Worked example 2 — find the missing rate

A ₹30 variety mixed with an unknown ₹ c variety in ratio 3 : 2 (cheaper : dearer) gives mean ₹28.

By cross: cheaper : dearer = $(30 - 28) : (28 - c) = 2 : (28 - c)$.

Set equal to 3 : 2 → $2 / (28 - c) = 3 / 2 \rightarrow 28 - c = 4/3$... re-check with parts below.

Cleaner: cheaper is 3 parts, so $(30 - 28) = 2$ matches the **dearer** "2" part → each part = 1; cheaper part $(28 - c) = 3 \rightarrow c = \text{₹}25$. ✓

Worked example 3 — ratio to hit a target price

At what ratio must ₹9 and ₹12 rice be mixed to sell at ₹10/kg?

$(12 - 10) : (10 - 9) = 2 : 1 \rightarrow \text{₹}9 \text{ rice} : \text{₹}12 \text{ rice} = 2 : 1$.

Quick table — mean of a 1 : 1 mix

Rate 1	Rate 2	Ratio	Mean
₹20	₹30	1 : 1	₹25
₹20	₹30	3 : 1	₹22.5
₹20	₹30	1 : 3	₹27.5



Whichever ingredient has the **larger share** pulls the mean **towards its own rate** — a handy sanity check.

④ Milk & Water Problems

A dealer stretches milk by adding water. Treat **water as the free (₹0) ingredient** and everything becomes alligation.

Key relations

- $\text{Water \%} = (\text{water} / \text{total mixture}) \times 100$.
- Milk : Water is just the quantity ratio in the vessel.
- Selling a milk-water mix at the **cost price of milk** $\rightarrow \text{Gain \%} = (\text{water} / \text{milk}) \times 100$.

Worked example 1 – water added

Given — 20 L of milk, then 5 L of water is added.

Milk : Water $\rightarrow 20 : 5 = 4 : 1$.

Water % $\rightarrow 5 / 25 \times 100 = 20\%$. 

Worked example 2 – sell at cost price of milk

A milkman mixes 2 L water in 10 L milk and sells at the **cost price of milk**.

He sells 12 L at the value of milk but paid for only 10 L. $\text{Gain} = 2 \text{ L of milk-value on } 10 \text{ L cost}$.

$\text{Gain \%} = (2 / 10) \times 100 = 20\%$. 

Worked example 3 – alligation for strength

How much water be mixed with 60 L pure milk so that water is 25% of the new mixture?

$\text{Water : Milk} = 25 : 75 = 1 : 3$. Milk (3 parts) = 60 L $\rightarrow 1 \text{ part} = 20 \text{ L} \therefore \text{water} = 20 \text{ L}$.

Milk : Water $\rightarrow$ Water %

4 : 1 $\rightarrow$ water = **20%**

3 : 1 $\rightarrow$ water = **25%**

3 : 2 $\rightarrow$ water = **40%**

5 : 3 $\rightarrow$ water = **37.5%**



Selling at cost price with water added $\rightarrow$ gain is measured **on the milk** (water/milk), **not on the whole mixture**.

Milk & Water – more work

Worked example 4 – find profit from a ratio

Milk : water in a can is 5 : 1 and the seller sells it at the cost price of milk.

Water : milk = 1 : 5 $\rightarrow$ Gain % = $(1/5) \times 100 = 20\%$.

Worked example 5 – water to reach a target gain

A trader has 40 L pure milk. How much water gives a 25% profit when sold at milk's cost price?

Gain% = water/milk $\times 100 = 25 \rightarrow$ water = 25% of 40 = **10 L**. Mixture = 50 L.

Worked example 6 – two cans, one target

Can A has milk : water = 4 : 1; can B has 2 : 3. In what ratio to mix for milk : water = 1 : 1?

Milk fraction: A = $4/5 = 0.8$, B = $2/5 = 0.4$, target $m = 0.5$.

A : B = $(0.5 - 0.4) : (0.8 - 0.5) = 0.1 : 0.3 = 1 : 3$.

Check $\rightarrow$ milk = $0.8 \times 1 + 0.4 \times 3 = 2.0$ over 4 L = 0.5 $\checkmark$.

Worked example 7 – add milk to change ratio

A 40 L mix has milk : water = 3 : 1. How much milk to make it 4 : 1?

Milk = 30 L, water = 10 L (water stays fixed). For 4 : 1 with 10 L water $\rightarrow$ milk = 40 L.

Extra milk needed = $40 - 30 = 10$ L.

Try these

Milk:water 6:1, sold at CP $\rightarrow$ gain **$16\frac{2}{3}\%$**

50 L milk, 10% profit $\rightarrow$ add **5 L** water

Milk:water 9:1, sold at CP $\rightarrow$ gain **$11\frac{1}{9}\%$**

25 L milk + 5 L water $\rightarrow$ water **$16\frac{2}{3}\%$**



When you only **add water**, the milk stays constant; when you only **add milk**, the water stays constant. Anchor on the unchanged part.

⑤ Repeated Replacement (Dilution)

Draw out some liquid, top up with water, repeat. Each round scales the pure liquid by the **same factor**.

Replacement formula

Vessel has x units of pure liquid; each time y units are drawn and replaced by water, done n times:

$$\text{Pure left} = x(1 - y/x)^n \quad \text{and} \quad \text{Pure : Total} = (1 - y/x)^n$$

Worked example 1 – the standard case

Given — $x = 40$ L pure milk, $y = 8$ L drawn & replaced with water, $n = 2$ times.

Factor $\rightarrow 1 - 8/40 = 1 - 1/5 = 4/5$.

Pure milk $\rightarrow 40 \times (4/5)^2 = 40 \times 16/25 = 640/25 = 25.6$ L.

Water $\rightarrow 40 - 25.6 = 14.4$ L. 

Worked example 2 – three rounds

100 L of wine; 20 L drawn & replaced with water, 3 times. Factor = $1 - 20/100 = 4/5$.

Wine left = $100 \times (4/5)^3 = 100 \times 64/125 = 51.2$ L. Water = 48.8 L.

Worked example 3 – find n

A vessel of 81 L milk becomes $16/81$ pure after replacing water repeatedly, 8 L each time... use ratio form.

$$(1 - y/x)^n = (2/3)^n = 16/81 = (2/3)^4 \rightarrow n = 4 \text{ rounds.}$$

Powers you'll reuse

$$(4/5)^2 = 16/25$$

$$(4/5)^3 = 64/125$$

$$(3/4)^2 = 9/16$$

$$(2/3)^3 = 8/27$$



The **total** volume never changes (you draw y and pour back y). Only the **pure** fraction shrinks by $(1-y/x)$ each round.

⑥ Mixing Two Mixtures

Two vessels already hold milk–water mixtures. To combine them, apply alligation to the **milk fractions** (or the water fractions).

Method

- Write each vessel's milk fraction: $a/(a+b)$ and $c/(c+d)$.
- Put them on the cross with the target fraction m in the middle.
- The cross gives the **ratio of the two vessels**.

Worked example 1 – equal quantities

Given — vessel A milk : water = 7 : 2, vessel B = 4 : 5; mixed in equal amounts.

Milk fractions → $A = 7/9$, $B = 4/9$.

Combined milk → $(7/9 + 4/9) \div 2 = (11/9)/2 = 11/18$; water = $7/18$.

Result → milk : water = **11 : 7**. ✓

Worked example 2 – find the mixing ratio

A is milk : water = 5 : 1, B is 3 : 5. In what ratio for a result of milk : water = 1 : 1?

Milk fractions: $A = 5/6$, $B = 3/8$, target = $1/2$.

$A : B = (1/2 - 3/8) : (5/6 - 1/2) = (1/8) : (1/3) = 3 : 8 \rightarrow$ **A : B = 3 : 8**.

Worked example 3 – combine given volumes

10 L of a 3 : 2 mix and 15 L of a 2 : 3 mix are poured together.

Milk = $3/5 \times 10 + 2/5 \times 15 = 6 + 6 = 12$ L; water = $4 + 9 = 13$ L.

Result milk : water = **12 : 13**. ✓



Always convert each vessel to the **same yardstick** – the fraction of milk (or of water) – before you apply the cross.



If quantities are given, skip the cross – just add milk to milk and water to water, then take the ratio.

⑦ Alligation for Other Averages

The cross works for **any weighted average** split into two groups — ages, speeds, marks, profit %. The two "rates" are the group averages; the ratio is the group sizes (or times).

General cross

Group1 : Group2 = (avg2 - overall) : (overall - avg1) — weights nearest to the overall win the larger share.

Worked example 1 — average age

Given — boys average 12 yr, girls average 10 yr, class average 11.5 yr.

Cross → boys : girls = (11.5 - 10) : (12 - 11.5) = 1.5 : 0.5 = **3 : 1**.

Check → $(12 \times 3 + 10 \times 1) / 4 = 46 / 4 = 11.5$ ✓. 

Worked example 2 — average speed (time ratio)

A car covers part of a trip at 30 km/h and part at 50 km/h, averaging 42 km/h.

Time at 30 : time at 50 = (50 - 42) : (42 - 30) = 8 : 12 = **2 : 3**.

Alligation on speeds gives the ratio of **times**, not distances.

Worked example 3 — average marks

Section X averages 75 marks, section Y averages 60, whole batch averages 69.

X : Y = (69 - 60) : (75 - 69) = 9 : 6 = **3 : 2** (number of students).



For **average speed** the weights are **times**; for classes/sections they are **head-counts**. Identify the weight before you cross.

Averages by Alligation – more

Worked example 4 – blended profit %

A man invests one part at 8% and another at 12%, earning 9% overall.

Part at 8% : part at 12% = $(12 - 9) : (9 - 8) = 3 : 1 \rightarrow 3 : 1$.

Worked example 5 – find the overall from a ratio

40 boys average 60 marks; 20 girls average 75. Batch average?

Overall = $(60 \times 40 + 75 \times 20) / 60 = (2400 + 1500) / 60 = 3900 / 60 = 65$ marks. 

Worked example 6 – average speed both ways

Equal distances at 40 km/h and 60 km/h. Average speed = harmonic mean = $2ab / (a+b)$.

= $(2 \times 40 \times 60) / (40 + 60) = 4800 / 100 = 48$ km/h.

Note – equal **distance** uses harmonic mean; equal **time** uses the simple average.

Worked example 7 – salary alligation

Average pay of officers ₹48000, of clerks ₹24000, of all staff ₹30000. Ratio of officers : clerks?

= $(30000 - 24000) : (48000 - 30000) = 6000 : 18000 = 1 : 3$.

Try these (group ratio)

avg 40, 50, overall 44 $\rightarrow 3 : 2$

5%, 8%, overall 6% $\rightarrow 2 : 1$

avg 20, 30, overall 26 $\rightarrow 2 : 3$

avg 12, 18, overall 15 $\rightarrow 1 : 1$



Alligation always gives a **ratio of weights**. To get actual counts you need one real number (total students, total investment...).

⑧ Adulteration & Gain %

A dealer sells at cost price but cheats on quality or quantity. The "free" adulterant (water, chalk) is pure profit.

Two standard results

- Adulterant added & sold at cost price $\rightarrow$ Gain % = (adulterant / genuine) $\times$ 100.
- False weight — sells at cost price but gives less: Gain % = (true — used) / used $\times$ 100.

Worked example 1 — water in milk

Given — 1 L water mixed into every 4 L milk, sold at milk's cost price.

Gain % $\rightarrow (1 / 4) \times 100 = 25\%$. 

Worked example 2 — false weight

A grocer sells at cost price but uses an 800 g weight for 1 kg.

Gain % = $(1000 - 800) / 800 \times 100 = 200 / 800 \times 100 = 25\%$. 

Worked example 3 — % of adulterant from gain

A trader mixes chalk in sugar and gains 20% selling at cost price. Find chalk : sugar.

$20 = (\text{chalk} / \text{sugar}) \times 100 \rightarrow \text{chalk} : \text{sugar} = 1 : 5 \rightarrow \text{chalk} = 16\frac{2}{3}\%$ of the mix.

Adulterant : genuine $\rightarrow$ gain

1 : 5 $\rightarrow$ gain **20%**

1 : 10 $\rightarrow$ gain **10%**

1 : 4 $\rightarrow$ gain **25%**

1 : 8 $\rightarrow$ gain **12.5%**



Gain is always measured **on the genuine part** (the cost he actually paid), never on the padded total.

Selling a Mixture at Profit / Loss

First find the **mean cost** of the mixture, then apply the ordinary profit-loss formula on that cost.

Profit on a mixture

Profit % = $(SP - \text{mean CP}) / (\text{mean CP}) \times 100$. Selling price of the whole = $SP/\text{unit} \times \text{total quantity}$.

Worked example 1 – rice blend sold for profit

Given — ₹30 and ₹40 rice mixed in ratio 2 : 3, sold at ₹42/kg.

Mean CP → $(30 \times 2 + 40 \times 3) / 5 = (60 + 120) / 5 = 180 / 5 = ₹36/\text{kg}$.

Profit % → $(42 - 36) / 36 \times 100 = 600 / 36 = 16\frac{2}{3}\%$. 

Worked example 2 – find SP for a target profit

₹80 and ₹100 tea mixed 3 : 2; the trader wants 20% profit. Find the selling rate.

Mean CP = $(80 \times 3 + 100 \times 2) / 5 = (240 + 200) / 5 = ₹88$. SP = $88 \times 1.20 = ₹105.60/\text{kg}$.

Worked example 3 – ratio for a target profit

In what ratio mix ₹60 and ₹65 pulses so that selling at ₹68.20 gives 10% profit?

Mean CP must be $68.20 / 1.10 = ₹62$. Cross: $(65 - 62) : (62 - 60) = 3 : 2 \rightarrow ₹60 : ₹65 = 3 : 2$.

Worked example 4 – a loss case

₹50 and ₹70 oil mixed 1 : 1, sold at ₹54/L. Mean CP = ₹60.

Loss % = $(60 - 54) / 60 \times 100 = 10\%$ loss.



Two-step drill → (1) mean CP by alligation / weighted average, (2) profit or loss on that CP.
Never mix the two steps.

More Solved Examples – I

Q1 – In what ratio must ₹15 and ₹20 rice be mixed to get ₹16.50/kg?

$$(20 - 16.5) : (16.5 - 15) = 3.5 : 1.5 = \mathbf{7 : 3}.$$

Q2 – 25% of a 40 L milk mix is water. How much milk to add to make water 20%?

Water = 10 L (stays fixed). For 20% water $\rightarrow$ total = $10 / 0.20 = 50$ L $\rightarrow$ add $50 - 40 = \mathbf{10}$ L milk.

Q3 – From 20 L pure milk, 4 L is replaced by water twice. Pure milk left?

$$20 \times (1 - 4/20)^2 = 20 \times (4/5)^2 = 20 \times 16/25 = \mathbf{12.8}$$
 L.

Q4 – Two alloys have gold : copper = 3 : 2 and 1 : 4. Mixed equally, gold : copper?

$$\text{Gold} = 3/5 + 1/5 = 4/5 \text{ over } 2 = 2/5; \text{copper} = 3/5. \text{ Ratio} = \mathbf{2 : 3}.$$

Q5 – Sugar at ₹15 and ₹20 mixed 3 : 2; sold at ₹21/kg. Profit %?

$$\text{Mean CP} = (15 \times 3 + 20 \times 2) / 5 = (45 + 40) / 5 = ₹17. \text{ Profit} = (21 - 17) / 17 \times 100 = \mathbf{23 \frac{9}{17} \%} \approx 23.53\%.$$

Q6 – A shopkeeper adds water to milk and gains 25% at cost price. Water : milk?

$$25 = (\text{water} / \text{milk}) \times 100 \rightarrow \text{water} : \text{milk} = \mathbf{1 : 4}.$$



Spot the type first: replacement $\rightarrow$ use the power formula; simple blend $\rightarrow$ use the cross; sale $\rightarrow$ find mean CP then profit.

More Solved Examples – II

Q7 – 60 kg alloy A (lead : tin = 3 : 2) and 100 kg alloy B (lead : tin = 1 : 4). Tin in the new alloy?
Tin = $2/5 \times 60 + 4/5 \times 100 = 24 + 80 = 104$ kg out of 160 kg $\rightarrow$ **65%** tin.

Q8 – A vessel is full of milk. 10 L is drawn, replaced by water; done twice; now milk : water = 81 : 19.
Capacity?
 $(1 - 10/x)^2 = 81/100 = (9/10)^2 \rightarrow 1 - 10/x = 9/10 \rightarrow 10/x = 1/10 \rightarrow x =$ **100 L**.

Q9 – Tea worth ₹126 and ₹135 mixed with a third at ₹x, ratio 1 : 1 : 2, mean ₹153. Find x.
 $126 + 135 + 2x = 153 \times 4 = 612 \rightarrow 2x = 612 - 261 = 351 \rightarrow x =$ **₹175.50**.

Q10 – How many kg of ₹9.60 sugar mixed with 24 kg of ₹14.40 to gain 20% by selling at ₹13.20?
Mean CP = $13.20/1.20 = ₹11$. Cross: $(14.4-11):(11-9.6) = 3.4 : 1.4 = 17 : 7$. Cheaper = $(17/7) \times 24 =$ **58 $\frac{2}{7}$ kg**.

Q11 – A can has milk & water 5 : 3. 16 L of the mix is removed and replaced by 16 L water; now 5 : 7. Capacity?
Let capacity be x. Milk after = $5x/8 - 5/8 \times 16 = 5x/8 - 10$; total stays x. $5x/8 - 10 = 5x/12 \rightarrow x/24 = 2 \rightarrow x =$ **48 L**.

Q12 – Two vessels A & B have milk : water = 4 : 3 and 2 : 3. Mix to get 1 : 1. Ratio A : B?
Milk fractions: A = $4/7$, B = $2/5$, target $1/2$. A : B = $(1/2 - 2/5) : (4/7 - 1/2) = (1/10) : (1/14) =$ **7 : 5**.

Higher-Level Solved Examples

H1 – 3 : 2 acid-water, part removed & replaced by water → 1 : 1. Fraction replaced?

Acid fraction $3/5 \rightarrow 1/2$. Removing fraction f : $3/5(1-f) = 1/2 \rightarrow 1-f = 5/6 \rightarrow f = 1/6$ of the mixture.

H2 – ₹20 rice mixed with ₹24 rice, then whole sold at ₹27.50 for 25% profit. Ratio?

Mean CP = $27.50/1.25 = ₹22$. Cross: $(24-22):(22-20) = 2 : 2 = 1 : 1$.

H3 – A container has 40 L milk. 4 L drawn & replaced by water, 3 times. Milk : water now?

Milk = $40(1 - 4/40)^3 = 40(9/10)^3 = 40 \times 729/1000 = 29.16$ L; water = 10.84 L → 729 : 271.

H4 – Average of 30 students is 40. If 20 boys average 35, girls' average?

Total = $30 \times 40 = 1200$; boys = $20 \times 35 = 700 \rightarrow$ girls (10) = 500 → average = $500/10 = 50$.

H5 – Wine : water = 3 : 1 in a cask. How much of the mix be replaced by water to make it 1 : 1?

Wine fraction $3/4 \rightarrow 1/2$. $3/4(1-f) = 1/2 \rightarrow 1-f = 2/3 \rightarrow f = 1/3$ of the mixture replaced.

H6 – ₹100 and ₹80 tea in ratio 3 : 2 is one blend; another is 1 : 1. Equal blends mixed → mean rate?

Blend-1 = $(100 \times 3 + 80 \times 2)/5 = ₹92$; blend-2 = ₹90. Equal amounts → $(92+90)/2 = ₹91/\text{kg}$.



"Replace a fraction once" → strength $\times (1-f)$. "Replace y units n times" → strength $\times (1-y/x)^n$. Same idea, different bookkeeping.

Practice Set

1. Mix ₹18 & ₹24 for mean ₹20 → ratio?
2. Mix ₹10 & ₹15 in 3 : 2 → mean?
3. 25 L milk + 5 L water → water %?
4. Milk:water 4:1 sold at CP → gain %?
5. 50 L milk, 8 L replaced by water once → milk left?
6. $x=40, y=10, n=2$ → pure liquid left?
7. Vessels 7:2 & 4:5 equal mix → ratio?
8. Boys avg 15, girls 12, class 14 → ratio?
9. Invest 6% & 10%, overall 7% → ratio?
10. ₹30 & ₹36 in 1:1, sold ₹36 → profit %?
11. Water in milk, gain 20% at CP → water:milk?
12. 800 g weight for 1 kg at CP → gain %?
13. ₹9.6 & ₹14.4 for mean ₹12 → ratio?
14. 81 L, replace 27 L by water once → wine left?
15. Avg speed of equal distances 30 & 60 → ?

Answer Key – with working

1 → 2:1 $((24-20):(20-18)=4:2)$ · 2 → ₹12 $((10 \times 3 + 15 \times 2) / 5)$ · 3 → 16⅔% $(5 / 30)$ · 4 → 25%
 $(\text{water} / \text{milk} = 1 / 4)$ · 5 → 42 L $(50 \times 42 / 50 = 50 \times 21 / 25)$ · 6 → 22.5 L $(40 \times (3 / 4)^2 = 40 \times 9 / 16)$ · 7 → 11:7 (milk
 11 / 18) · 8 → 2:1 $((14-12):(15-14))$ · 9 → 3:1 $((10-7):(7-6))$ · 10 → 9 1/11 % $(\text{CP } 33, (36-33) / 33)$ · 11 → 1:5
 $(20 = w / m \times 100)$ · 12 → 25% $(200 / 800)$ · 13 → 2:1 $((14.4-12):(12-9.6)=2.4:2.4 \rightarrow 1:1)$ · 14 → 54 L
 $(81 \times (1 - 27 / 81) = 81 \times 2 / 3)$ · 15 → 40 km/h $(2 \times 30 \times 60 / 90)$.

*Note Q13: $(14.4-12):(12-9.6) = 2.4 : 2.4 = 1 : 1$ (equal parts).

Quick Revision

- ✓ Cross → cheaper : dearer = $(d-m) : (m-c)$. Mean price = total cost / total quantity.
- ✓ Replacement → pure left = $x(1-y/x)^n$. Sell at CP with water → gain = water / milk $\times 100$.
- ✓ Same cross fits ages, speeds, marks & profit % — any two-group weighted average.

☆ Mix it right — alligation makes it easy! ☆